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***A COMPARATIVE ANALYSIS OF TRANSPORTATION PROBLEM UNDER FUZZY AND  
PROBABILISTIC UNCERTAINTIES***

**Ahongshangbam Nehru Singh, Research Scholar, Department of Mathematics, School of  
Science, Glocal University, Saharanpur.**

**Dr Uma Shanker, Associate Professor, Department of Mathematics, School of Science,  
Glocal University, Saharanpur.**

**ABSTRACT**

A significant issue that has received extensive study in the field of operations research is the transportation problem. It has been researched to model various problems from actual life. Particularly important is the applicability of this Problem in NP-Hard Problems. Here, we compare how the Transportation Problem is handled by probabilistic and fuzzy uncertainties. For reasoning under uncertainty, fuzzy logic is a computer paradigm that generalizes traditional two-valued logic. This requires that the notation of membership in a set be transformed into an issue of degree. By doing this, we achieve two goals: (i) making it easier to describe human knowledge including nebulous notions, and (ii) improving our capacity to come up with affordable solutions to real-world issues. Fuzzy Sets' multi-valued structure makes it possible to handle ambiguous and hazy information. It is a model-free strategy that cleverly masks probability theory. We compare the simulation results from the two methods and talk about computational complexity. This is the first analysis of the Transportation Problem using Probabilistic and Fuzzy Uncertainties that we are aware of. A special type of linear programming problem is the transportation problem. It has received a lot of attention in the fields of logistics and operations management, where getting products from producers to consumers is a crucial concern. By rephrasing the Distribution Problem as a generalization of the traditional Transportation Problem, distributor decision-making can be made as efficiently as possible. The traditional transportation problem can be visualized as an objective function subject to constraints within a mathematical structure. The traditional method calls for minimizing transportation expenses from M suppliers or wholesalers to N destinations or customers. It is an optimization problem that has been used to address a number of NP-Hard issues.

***KEYWORDS: Operations Management, Transportation, Human Knowledge, Ambiguous***

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## 1. INTRODUCTION

In today's world, transportation plays an important role in everyone's life. It is not showing its impact only on economic status but also improving the quality of life. Transportation devices provide the way for goods, products, people to be transferred from one location to another with an ease in both cost and time. Only the big cities having contemporary life is suffering from the problems associated with traffic jamming. Thus, transportation is a significant element of our lifestyle and in order to function efficiently, solving transportation problems is necessary as this will lead to productive finance, well managed transport so that all developmental goals related to transportation system can be attained. The government is dealing with the huge tasks to solve mobility issues at different levels. Transportation problems have been reviewed by S. Datta in the emergent nations. Transportation problem belongs to the problem of Linear programming problem, handling the allocation into different areas of need of individual items (finished or raw), in a way which minimises the entire costs of transportation, personal experience is exactly how people, such as drivers, riders, bikers or maybe pedestrians, percept and comprehend road environments, passenger terminals or perhaps IT systems in some elements of transport engineering.

In certain areas of transport engineering, the concept of customer experience is possibly used for a long time, for instance, while studying the 'level of service' or even in evaluating user satisfaction by survey outcomes. In spite of that, there are still missing actions that define whether the consumers are happy or they have encountered any inconvenience. Moreover, sole production of all effective measures or Measure of Effectiveness (MOEs) required for examining effective transportation and the entire transportation system is done virtually without focusing on the techniques like Artificial intelligence.

In the beginner, the model was formulated so it is called the transportation issue for deciding the ideal shipping pattern. To transport a particular good/product or services of all  $n$  origins  $i = 1, 2, 3, \dots, n$  to any of  $m$  destinations  $j = 1, 2, 4, \dots, n$  is the conventional, extremely common transportation problem. The beginnings are production services with capacity  $a_1, a_2, a_3, \dots, a_n$ , and end point (destination) is also depository (warehouse) with  $ph$  levels needed for  $b_1, b_2, b_3$  and... $b_n$  requires. A cost  $c_{ij}$  is given for the product's transport of the defined item from the resource  $i$  to the place  $j$  without any loss of

generality,

$$c_{ij} \geq 0 \forall i, j$$

Hence, one should identify the amounts  $x_{ij}$  being moved from sources  $I = 1, 2, 3, \dots, n$  to endpoints  $j = 1, 2, 3, \dots, m$  in such a manner that the entire price is lessened.

$$\text{Minimize } Z = \sum_{i=1}^m \sum_{j=1}^n c_{ij} x_{ij}$$

Conditions

$$\sum_{j=1}^n x_{ij} \leq a_i \quad i = 1, 2, \dots, m \quad (\text{Row restrictions})$$

$$\sum_{i=1}^m x_{ij} \leq b_j \quad j = 1, 2, \dots, n \quad (\text{Column restrictions})$$

$$x_{ij} \geq 0 \quad \forall i \text{ and } j$$

$$\sum_{i=1}^m a_i = \sum_{j=1}^n b_j \quad ((\text{Balanced condition}))$$

Transportation problem (TP) belongs to linear problems subclass, handling the transportation from a few sources (producing, or gracefully centring) of a solitary homogeneous substance into many sinks (destinations or distribution centers). Although the practitioner tends to a TP, at any point of demand he usually has a certain limit and a given requirement. The aim of TP is to reduce the overall transportation expense while fulfilling flexibly and demand constraints by the quantities shifted from the origin to the destination.

### 1.1 Cost Minimizing Transportation Problem

Assume that  $m$  sources (i.e., production lines where the wares are fabricated) contain different measures of uniform (homogeneous) wares which must be assigned to  $n$  destinations (i.e., markets where the wares are to be distributed). It is expected that the total demand equivalents to the total flexibly, that is

$$\sum_{i=1}^m a_i = \sum_{j=1}^n b_j$$

Other than the provisions and demands,  $a_i$  and  $b_j$ , which are non-negative, it is additionally given a lot of delivery costs  $c_{ij}$ , which might be unhindered (as a rule non-negative). The problem is to decide the

measure of units to be sent from  $i$ th source to  $j$ th destination all together that reserves will be exhausted and prerequisites are satisfied at a general minimum cost. If  $x_{ij}$  is the measure of product moved from  $i$ th starting point to  $j$ th destination then the mathematical form of the problem is to

$$\text{Minimize } Z = \sum_{i=1}^m \sum_{j=1}^n c_{ij} x_{ij}$$

Subjecting to the conditions

$$\sum_{j=1}^n x_{ij} = a_i; \quad i=1, 2, \dots, m$$

$$\sum_{i=1}^m x_{ij} = b_j; \quad j=1, 2, \dots, n$$

$$x_{ij} \geq 0 \quad a_i > 0, \forall i \in I; \quad b_j > 0, \forall j \in J$$

$i = \{1, 2, \dots, m\}$  = set of indices of supply points

$j = \{1, 2, \dots, n\}$  = set of indices of demand points

Be that as it may, if the total accessibility of an item from each source not been equivalent to the entire demand required by end points, then the problem goes under the lopsided transportation problem. It might happen in two different forms:

- i. Excess of availability i.e.,

$$\sum_{i=1}^m a_i > \sum_{j=1}^n b_j$$

- ii. Shortage in availability

$$\sum_{i=1}^m a_i < \sum_{j=1}^n b_j$$

It can be made balanced by inserting a dummy demand when  $\sum_{i=1}^m a_i > \sum_{j=1}^n b_j$  or dummy supply when  $\sum_{i=1}^m a_i < \sum_{j=1}^n b_j$  with the associated shipping cost zero.

### 1.2 Transportation Problem for minimization of cost with Mixed Restrictions/ Constraints

Watching the idea of providers in down to earth life, it is seen that the providing limit of the gracefully focuses doesn't stay constant all through, because of the abundance and deficiency of labor, hardware, crude materials, and so forth., engaged with production. That is, the providing limit of the makers varies. On a specific second, it doesn't influence the providing limit of certain makers and they can gracefully a fixed measure of products. At a similar second, when lack experiences, a few sources wish to flexibly not exactly a fixed measure of items. While in the event that, when abundance of

products is accessible, a few sources are in position to gracefully in excess of a fixed sum.

### **1.3 Transportation Problem for the minimization of time**

The issue of the total cost reduction of transportation is focussed since long and is notable. Be that as it may, in the advanced age, individuals feel that time has extraordinary value when contrasted with money. As time can be utilized to bring in money however money can't be utilized to buy additional time. Money, once gone, can be recuperated however they sat around idly can't be recovered.

According to the celebrated maxims, "One thing you can't reuse is sat around idly." - Anonymous "To pick time is to spare time." - Francis Bacon Thus, in transportation, time included is for the most part liked to be limited when contrasted with cost. The Time Minimizing Transportation Problem (TMTP) is to decide the measure of a product moved from a source to the individual destination satisfying the given flexibly and demand limit with the goal that the transportation work is to be finished in minimum time.

## **2. LITERATURE REVIEW**

**Kumar and Kumari (2018)** a method, specifically zero suffix strategy is recommended to solve the transshipment problems with several constraints. Constant transshipment style in which the foundation and destination restrictions is actually composed not only of the equality indication but in addition of greater than or possibly the exact same as, or perhaps under or possibly identical to like constraints, is known as as transshipment problems with several constraints. The classical transportation concern is following solved by 0 suffix strategy. The cure tested through modi indices declares an optimum fix. Strategy is organized at the kind of algorithm and illustrated by means of a numerical illustration.

**Dhodiya as well as patel (2017)** Solving multiple interval problems by using the concept of grey scenario choice based on grey figures In addition to impartial abilities like cost, time, etc., an interval transportation issue constructs information on supply in several intervals. The idea of the best limit, left middle, half width and interval limit could be turned into a classical MOTP. Multi-target transportation interval, mass selection, successful solution, impact measurement, gray situation.

**Juman, Nawarathne and Z., Shashini (2019)** the establishment of a Feasible Preliminary Solution (IFS) for a transportation problem is essential for the acquisition of a very comprehensive transport money remedy. Better first practical remedy is able to stick to a small full price solution for a smaller

number of iterations. The JHM only considers column fines. This paper proposes a brand-new strategy with row sanctions to identify AN IF for a transportation issue. A numerical illustration illustrates the brand-new technology. The brand-new methodology demonstrates a comparative study on a number of benchmarks that each of the problems, except one, can be accurately or possibly replied to better. This would allow us to consider our new approach as an alternative way of sticking to a viable preliminary response to a transportation issue.

### 3. MATHEMATICAL STRUCTURE OF THE TRANSPORTATION PROBLEM

In order to illustrate the next situation, the transportation issue has been mathematically organized. The purchase of a homogeneous device can be done as 'l' known quantity (recognized numbers) and identical devices' origins are required at each of 'm' destinations. We know the transportation amount of moving the single product from the source to the destination. The schedule for transportation should be decided first that will satisfy desired resources availability, destination requirements and other non-negative restrictions along with the reduction in the whole cost of transportation. Mathematically, the problem can now be described as:

$$\text{Minimize } z = \sum_{i=1}^l \sum_{j=1}^m c_{ij} x_{ij}$$

Subjecting to the restrictions,

$$\sum_{j=1}^m x_{ij} = a_i \text{ for } i = 1, 2, \dots, l$$

$$\sum_{i=1}^l x_{ij} = b_j \text{ for } j = 1, 2, \dots, m$$

$$\sum_{i=1}^l x_{ij} = b_j \text{ for } j = 1, 2, \dots, m$$

$$x_{ij} \geq 0 \text{ for } i = 1, 2, \dots, l \text{ and } j = 1, 2, \dots, m$$

Assuming,

$$\sum_{i=1}^l a_i = \sum_{j=1}^m b_j$$

The twofold transportation issue is defined as:

$$\text{Maximize } F = \sum_{i=1}^l a_i u_i + \sum_{j=1}^m b_j v_j$$

Subjecting to the conditions,

$$u_i + v_j \leq c_{ij}, \text{ for } i = 1, 2, \dots, l \text{ and } j = 1, 2, \dots, m$$

Where  $u_i$  and  $v_j$  are unrestrained in sign for all  $l$  and  $j$ .

#### 4. MULTI-OBJECTIVE OPTIMIZATION PROBLEM

Various problems in real world optimisation are multiple goals which are simultaneously optimized by a typical set of constraints. Probably the most standard multi-target mathematical model and are simultaneously optimized by a common set of constraints. A productive availability-based strategy for multi-target enhancement appropriate to the plan of marine secured region networks is depicted. Multi-target network advancement featured beforehand unreported advance changes in the construction of ideal subnetworks for assurance related with negligible changes in cost or advantage capacities. This underlines the allure of playing out a full, unconstrained, multi-target enhancement for marine spatial arranging. Best power techniques, analyzing all potential blends of ensured and unprotected locales for an organization of destinations, are unfeasible for everything except the littlest organizations as the quantity of potential organizations develops as  $2m$ , where  $m$  is the quantity of locales inside the organization. A metaheuristic strategy based around Markov Chain Monte Carlo strategies is portrayed which looks for the arrangement of Pareto ideal organizations (or a decent guess thereto) given two separate target capacities, for instance for network quality or adequacy, populace determination, or cost of assurance. The advancement and search techniques are free of the decision of target works and can be handily reached out to multiple capacities. The speed, exactness and combination of the technique under a scope of organization designs are tried with model organizations dependent on an augmentation of arbitrary mathematical charts. Assessment of two genuine marine organizations, one assigned for the assurance of the stony coral *Lophelia pertusa*, the other a theoretical man-made organization of oil and gas establishments to ensure hard substrate biological systems, shows the force of the strategy in finding multi-target ideal answers for organizations of up to 100 destinations. Results utilizing network normal briefest way as an intermediary for populace versatility and quality stream inside the organization upholds the utilization of a protection system

based around exceptionally associated bunches of destinations. Perhaps the most standard multi-objective optimization problem mathematical model is:

$$\text{Maximize } F(X) = [f_1(X), f_2(X), \dots, f_m(X)],$$

$$X = (x_1, x_2, \dots, x_n)$$

Subject to:

$$g_j(X) \leq 0, \quad j = 1, 2, \dots, k$$

$$h_j(X) = 0, \quad j = 1, 2, \dots, m$$

$$l_j(X) \geq 0, \quad j = 1, 2, \dots, r$$

Wherever  $f_1, f_2, \dots, f_m$  will be the objective features, Variables  $x_1, x_2, \dots, x_n$  belong in the choice variables as well as  $X$  is known as choice vector. The multi-objective programming problem can also be named.

## 5. FUZZY SET THEORY

Fuzzy sets are those sets whose elements have membership function. An element may or may not belong to the set; a response may or may not be possible in optimizations. Precision assumes that the unit parameters exactly reflect either our interpretation of the modeled phenomenon or the characteristics of the actual system.

Vague, that is, the difficulty of making a precise or sharp distinction, is among the implications attributed to the word ambiguity. This is relevant to countless expressions that we used frequently in our day-to-day life such as expensive homes, set of all intelligent girls, exceptionally reputed universities. This specific deception is a distinctive feature of natural language and doesn't specify impreciseness.

The concept of fuzzy set is used in representing/depicting uncertainties, though the principle of probability is still the prominent method of representing uncertainty in the mathematical models. Because of this, many uncertainties remained in the standards of random unreliabilities. The principle based on Fuzzy set is regarded to be a tremendous tool to model the anxiety type with less accuracy related to vagueness, even with very less information in hand.

The essential transportation problem applied to any ordinary distribution situation in which there are various demand points, each with known prerequisites for an offered product, to be provided from



various gracefully points, every one of which has a known accessibility of this product. Connecting the flexibly and demand points are various potential routes, every one of which has a distribution cost. The objective is to decide the distribution design which will limit total transportation cost. In other words, we are attempting to choose how much product ought to be delivered over every conceivable course to satisfy all demand points necessities while not surpassing the accessibility limitations of any gracefully point. Can there be many points of starting  $D_n$  with  $(b_j > 0)$ ,  $j=1, 2, \dots, n$  preconditions individually,  $O_1, O_2, \dots, O_m$  with  $(a_i > 0)$ ,  $i=1, 2, \dots, m$  accessibility units separately and  $n$  destinations  $D_1, D_2, \dots$ . If  $X_{ij} > 0$  is a measure of an item to be sent from its source to the  $j$ th destination, the aim is to settle on  $x_{ij}$ 's to restrict the total cost ( $z$ ) of transportation to meet all accessibility and requirement constraints. The problem of Transportation can be defined as follows:

#### **6. LINEAR PROGRAMMING**

Decision-production assumes a crucial job in everyday exercises. Multidimensional and with many aims - corporate, economic, environmental, social and specialized - are the main characteristics of the present problems in decision-making. Due to the erratic future, a part of the vulnerability often torse precise decision-making. Since the challenges of people's decision-making are multidimensional and no single dimensional, multi-target approaches have to be taken. One of the most important procedures for an organizational review is linear programming.

#### **7. RANKING FUNCTION**

Ranking fuzzy numbers is a significant tool in decision-making. Making decisions including multiple objectives is day by day task for many individuals in the more assorted fields, and consequently multiple objective decision-making problems have accepted significance in the overall area of decision-making theory. Ranking fuzzy numbers is utilized for decision-making forms in an unfriendly economic environment. In powerfully growing organizations, different exercises, for example, arranging, execution, and other procedures occur continuously.

#### **8. FUZZY TECHNIQUES AND ITS APPLICATIONS FOR THE DECISION-MAKING PROCESS IN VARIOUS FIELDS ESPECIALLY IN TRANSPORTATION PROBLEM**

One of the main problems of linear programming in some real situations is the transportation problem (TP). The writing has also drawn considerable interest. The main purpose of TP is to deliver products

to certain destinations from specific sources, thereby reducing the overall cost of transportation. The transportation issue involves some genuine applications, such as planning, manufacturing, venture, plant position and stock management, etc. The old-style TP has some limitations to plan genuine TP problems through a single objective feature.

The data is crisp in nature in the case of conventional transportation problems. Nevertheless, a large part of the cases given are in fact imprecise in circumstances. In our formulated model, this imprecise nature is calculated by a fuzzy number. The  $\alpha$ -slice representation was also shown which is proportional to the extension standard definition. In order to use T2FSs for transportation problems, important operations for fuzzy sets will be required.

## 9. CONCLUSION

The possibilities of the outlined research based on the main aims of the research are listed below:

- a. A fluid logic methodology is built for the analysis of the user's perception of transport problems on the basis of research on the user's perception of transport problem and on its programme.
- b. At present, transport is an essential element, playing a key role in the advancement of economy. Solid and appropriately coordinated vehicle administrations are needed for an expert presentation of industry, development and horticulture.
- c. Reliable and appropriately coordinated vehicle administrations are needed for an expert presentation of industry, development and agribusiness. The public state of mind and effectiveness of work likewise to a great extent rely upon the important elements of a painstakingly picked transport framework. A consistent expansion in transportation is joined by developing requests for a better of transport administrations and ideal proficiency of transport execution. Presently, joint endeavors taken by the vehicle specialists and overseeing organizations of the nation are needed to create and upgrade the presentation of the public vehicle framework directing hypothetical and exact examination.
- d. Advanced fuzzy software, with a comprehensive implementation and application related to the fluctuating system, includes the development of fluid membership features.
- e. In transport problems related to, transport problem user perceptions, the fluctuating methods built are used.

- f. The very first program is an examination with the fuzzy aggregating approach of the service level of the different message signs.
- g. Medium security evaluation by using a hierarchical, fuzzy inference method based on expert opinion.
- h. Validation methods and the results of fuzzy tactics are designed and applied to two individual concerns relating to consumer perceptions of transportation problems.
- i. The two transport issues are the study of program efficiency of the assessments and the signaling of mean safety intersections on motorway roads and superhighways, that vary quite from the issue of protection mentioned above. These validations compare the non-fuzzy, traditional methods to deal with those issues.
- j. The validation performed herein deviates a little from more conventional approaches due to the serious difficulties of validating user perception.

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